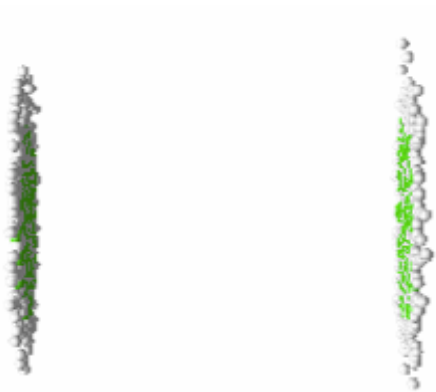




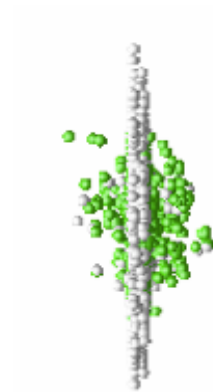
Comparing energy loss phenomenology in a hot dense medium

Marta Verweij
Utrecht University
BND School 2009
19-09-2009

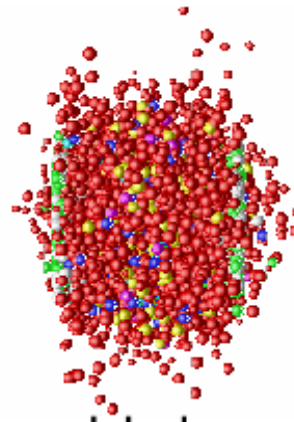
Heavy ion collision



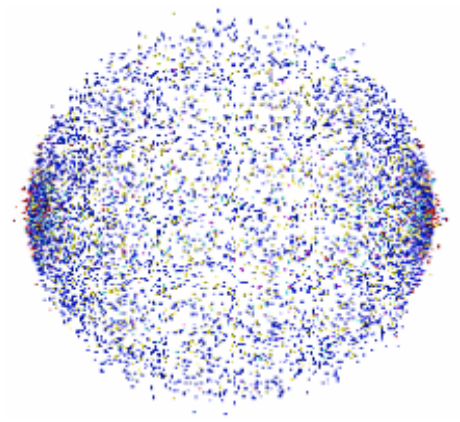
Colliding
nuclei



Hard
scattering



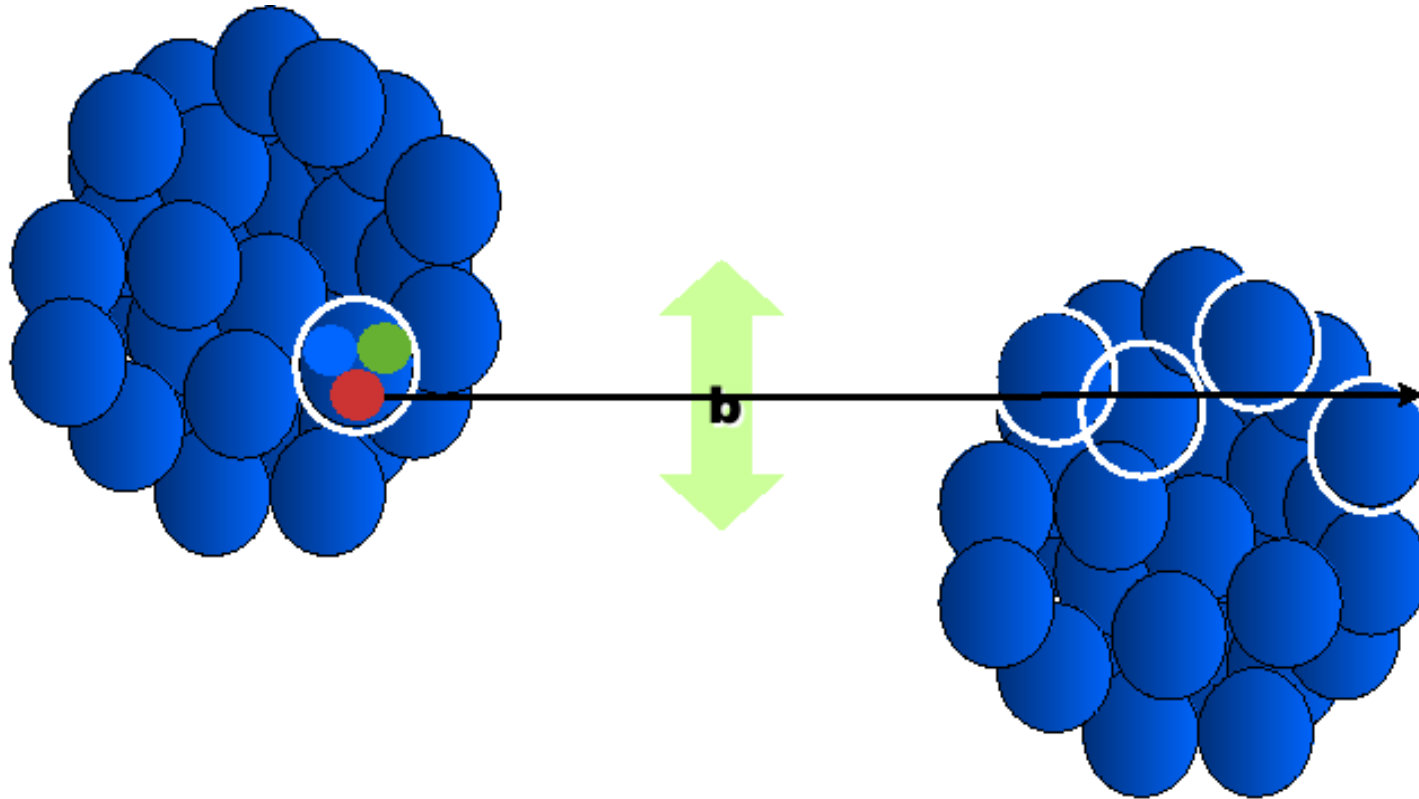
Holy
Grail



Final hadrons

Heavy ion collision

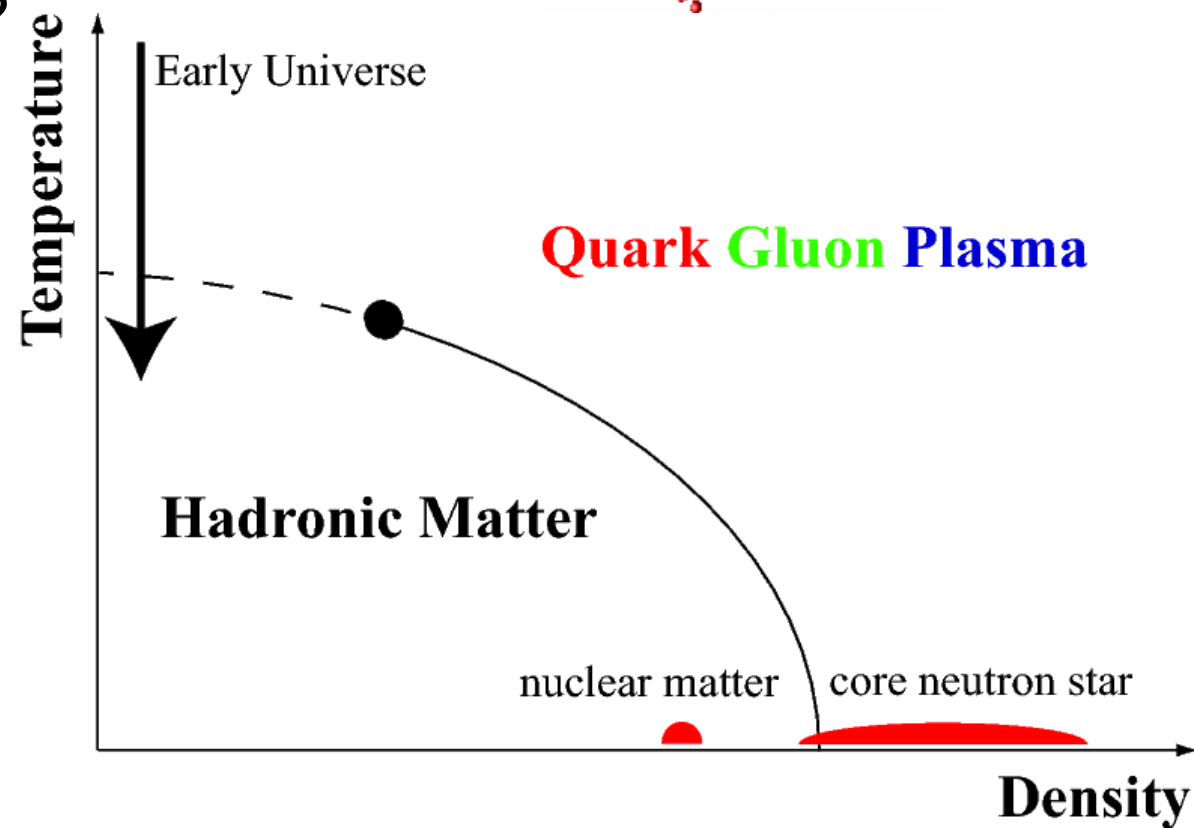
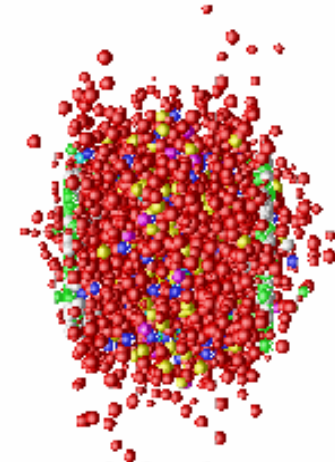
Hard scattering



- Many independent hard scatterings.

Hot dense medium

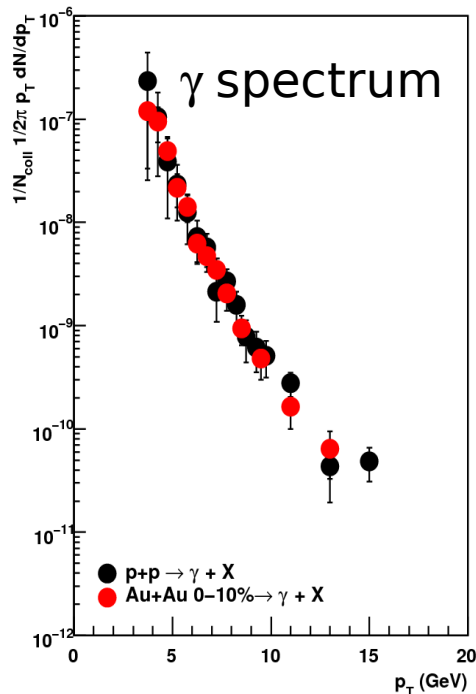
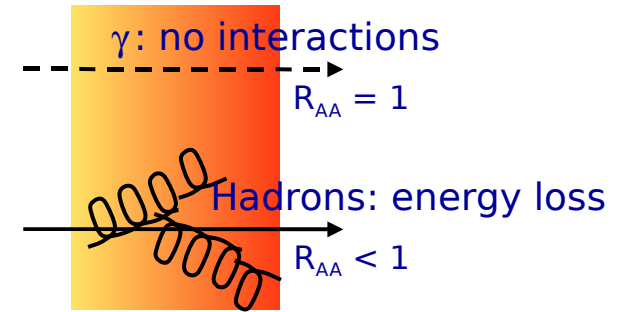
- What is the density of the medium?
- Energy density of the medium?
- Viscosity of the medium?
- Quark Gluon Plasma?
- Phase transition?
- Equation of state?



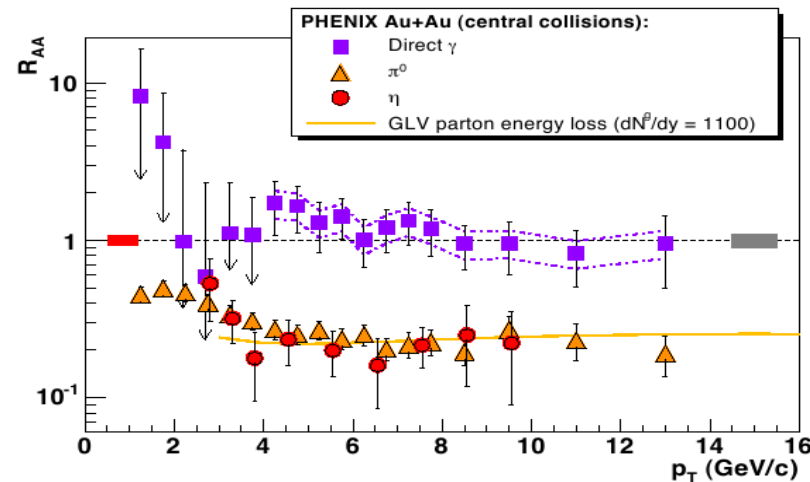
Nuclear Modification Factor

$$R_{AA} = \frac{dN/dp_t|_{Au+Au}}{N_{coll}dN/dp_t|_{p+p}}$$

- Yield per collision relative to p-p



PHENIX, PRL 94, 232301

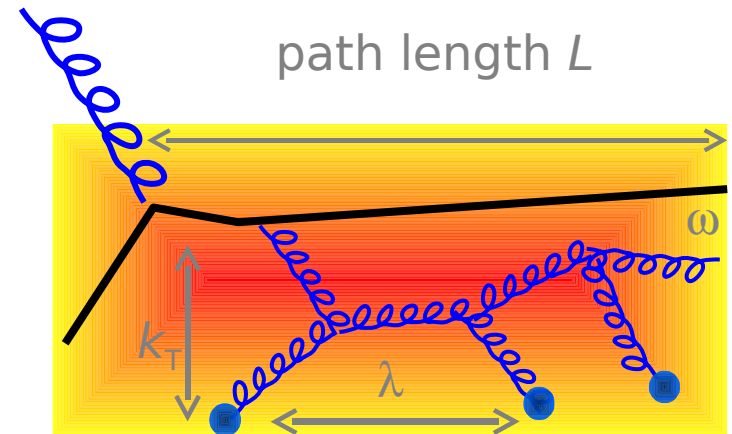


- High p_t hadrons strongly suppressed.
- Direct photons scale with N_{coll} .
- A+A is superposition of p+p

Energy loss in hot dense medium

- Parton traversing medium radiates gluons.
- Medium characterized by:
Transport coefficient

$$\hat{q} = \frac{\langle k_t^2 \rangle}{\lambda}$$



$$\frac{dN}{dp_{t,hadr}} = \frac{dN}{dp_{t,parton}} \circ P(\Delta E) \circ D(p_{t,hadr}/p_{t,parton})$$

Measurement	Input parton spectrum Known LO pQCD	Energy loss Has to be calculated	Fragmentation Factor Known from e+e-
-------------	---	--	---

Energy loss models

- Multiple Soft Scattering Approximation:
many interactions
Input parameters: q_{hat} and L
- Opacity Expansion:
few hard interactions
Input parameters: μ and λ
- Both have an energy loss probability distribution.

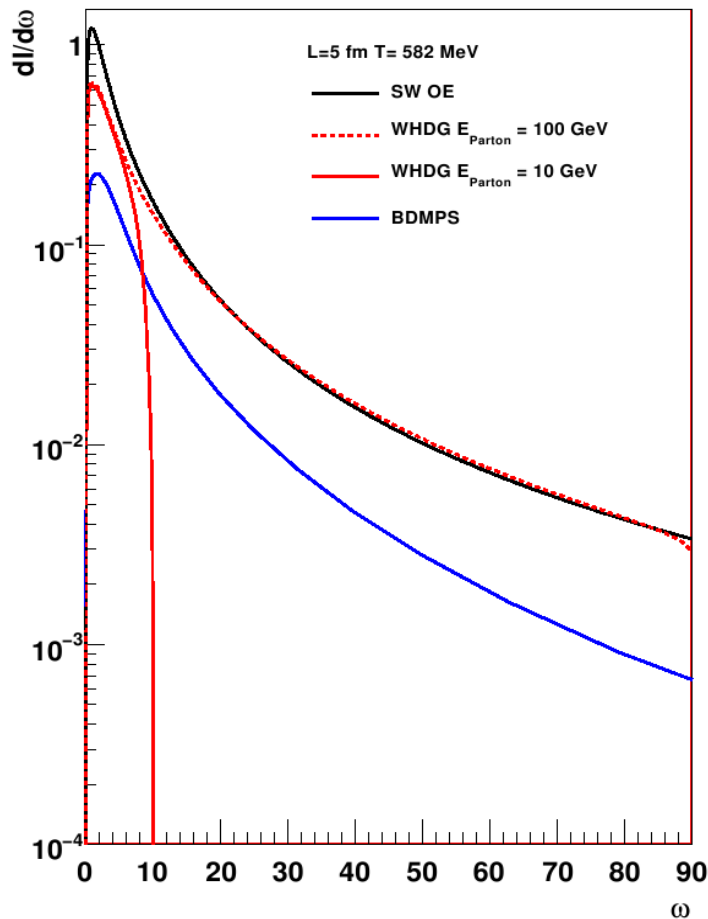
TECHQM Brick Problem

Theory-Experiment Collaboration for Hot QCD Matter

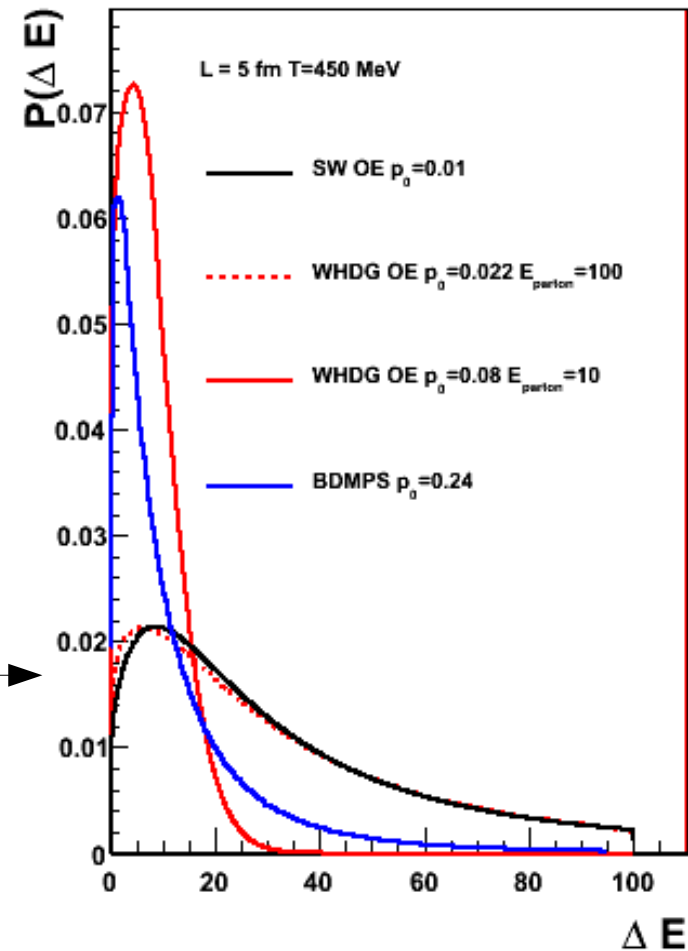
- Brick: fixed length L and temperature T .
- Parton of energy E is shot through brick.
- **Apple-to-apple** comparison of:
 - Multiple Soft Scattering (ASW-BDMPS) *Phys.Rev.D68 014008*
 - Opacity expansion:
 - ASW-SH *Phys.Rev.D68 014008*
 - WHDG radiative *Nucl.Phys.A784 426*
- **Input parameters are calculated from T .**

Brick examples

- Single gluon emission spectrum



- Energy loss distribution

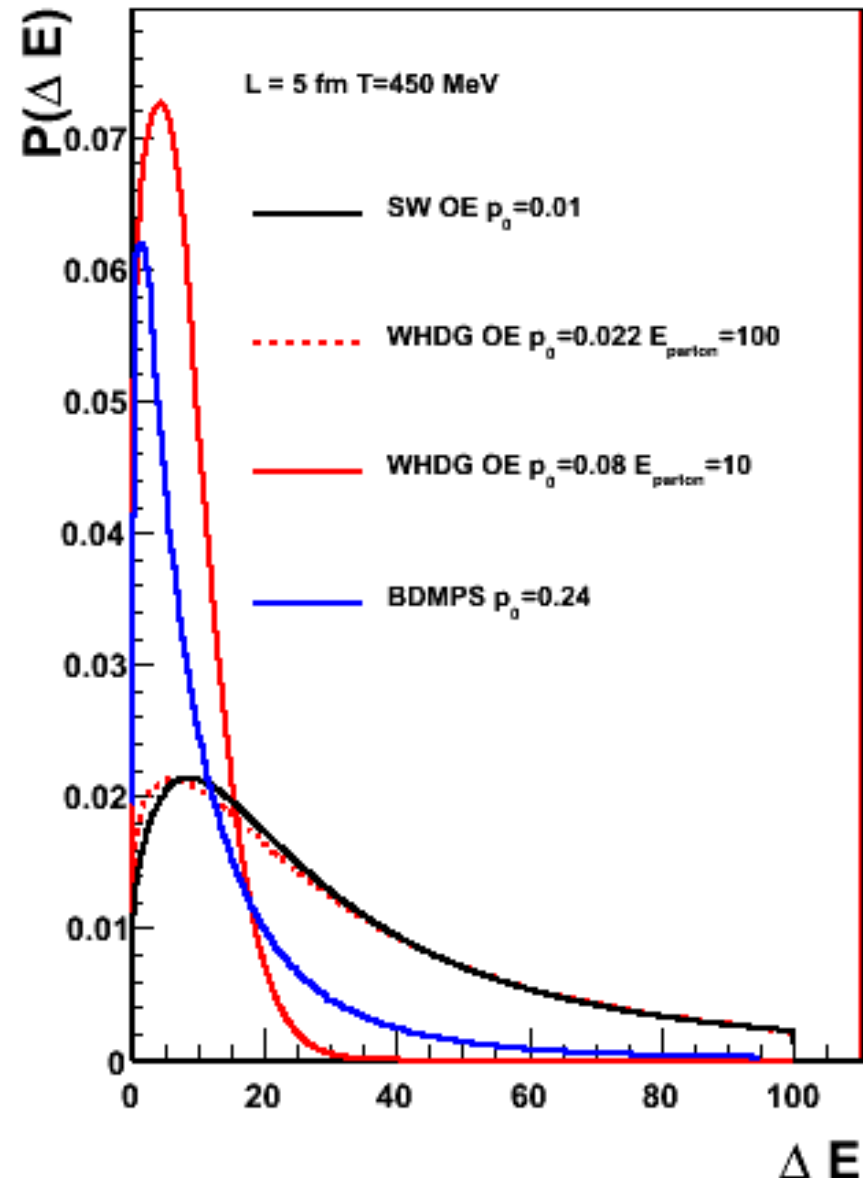


Poisson convolution gives multiple gluon spectrum



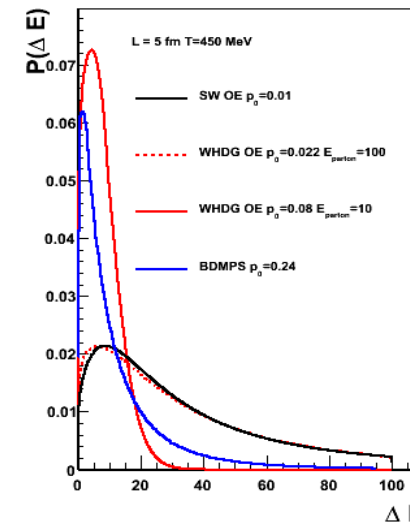
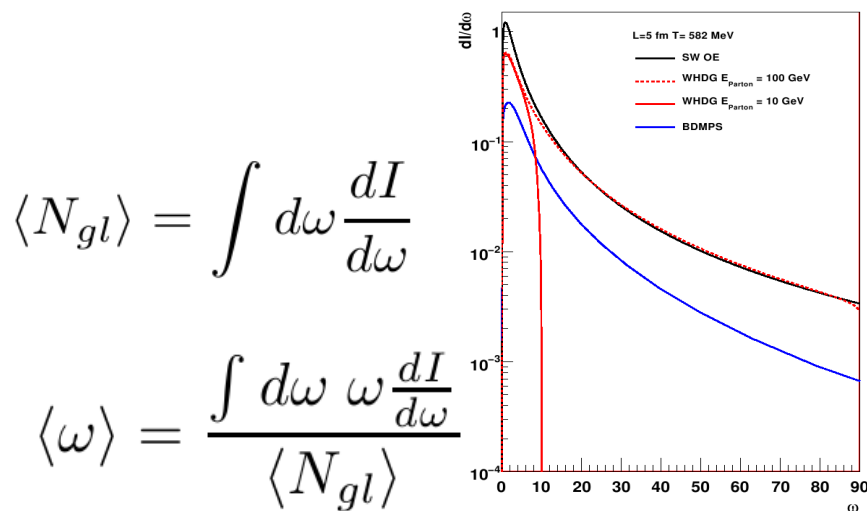
Energy loss probability distribution

- $P(\Delta E)$:
 - Continuous part
 - Discrete part
- Large differences between models under same medium conditions.



How much energy do we lose?

- Single gluon spectrum
- Energy loss distribution



	$\langle N_{gl} \rangle$	$\langle \omega \rangle$ (GeV)	$\langle \Delta E \rangle$ (GeV)
BDMPS	2.0	13	3.4
WHDG (E=10 GeV)	3.0	3.2	5.4
WHDG (E=100 GeV)	5.3	12	8.1
SWOE	7.2	9.8	9.0

→ for $E_{\max} = 10$ GeV

- Large difference between BDMPS and OEs!**

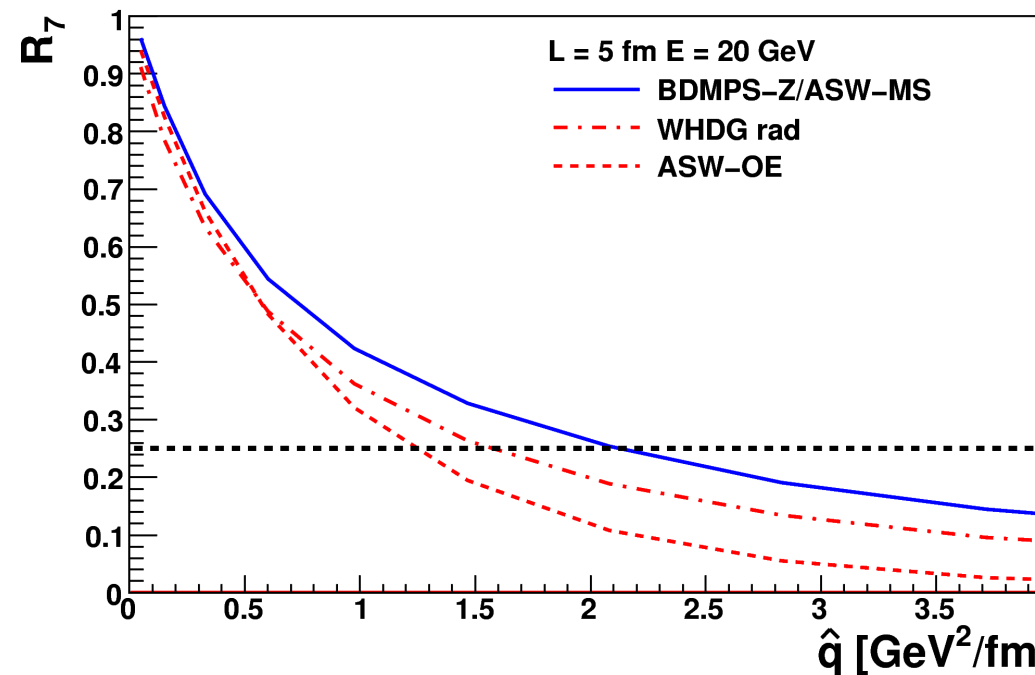
Suppression in a brick

- R_7 is an approximation for R_{AA} .

$$R_n = \int_0^1 d\epsilon (1 - \epsilon)^{n-1} P(\epsilon)$$

$$\epsilon = \Delta E / E$$

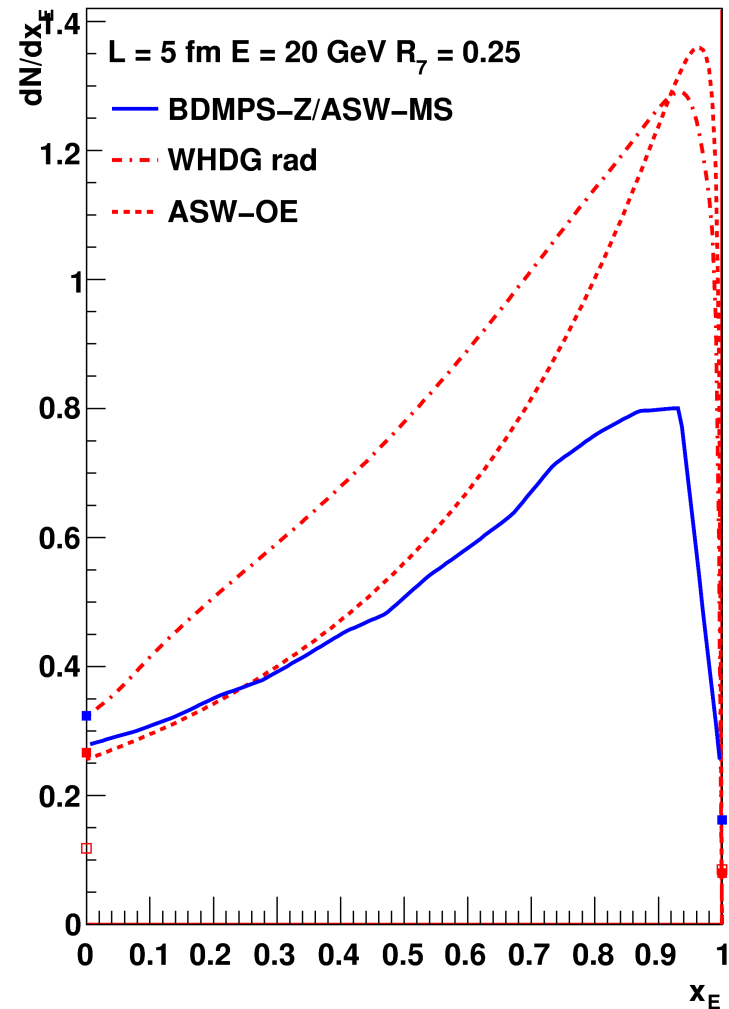
- Roughly factor 2 difference in $\hat{q}$ for same suppression.



$R_7=0.25$	$\hat{q}$ (GeV ² /fm)	T (MeV)
BDMPS	2.13	400
ASW-OE	1.25	360
WHDG	1.58	330

Outgoing quark spectrum

- $x_E = 1 - \Delta E/E$
- $x_E = 0$: Absorbed quarks
- $x_E = 1$: No energy loss
- *Black-white* scenario for BDMPS



“Realistic” Geometry

- Parton spectrum: LO pQCD T. Renk
- Energy loss: BDMPS and WHDG
- Fragmentation: KKP

“Realistic” Geometry

- Parton spectrum: LO pQCD T. Renk
- Energy loss: BDMPS and WHDG

- Optical Glauber:

- Density profile of medium

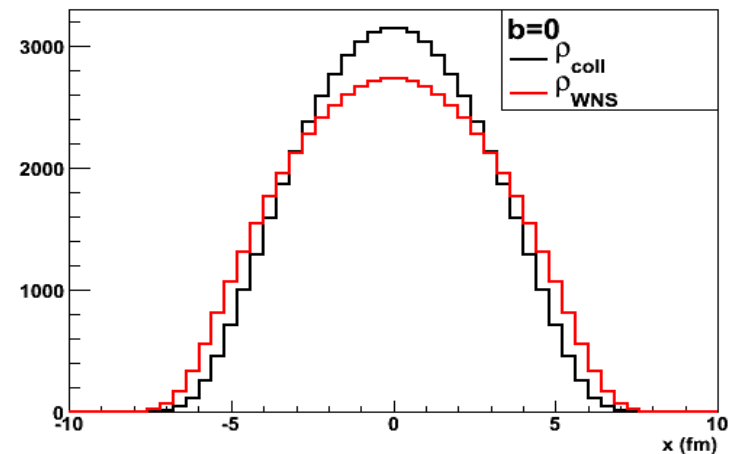
- Collisional scaling:

$$\rho_{coll} = k_{coll} \times T_A T_B$$

- Participant scaling:

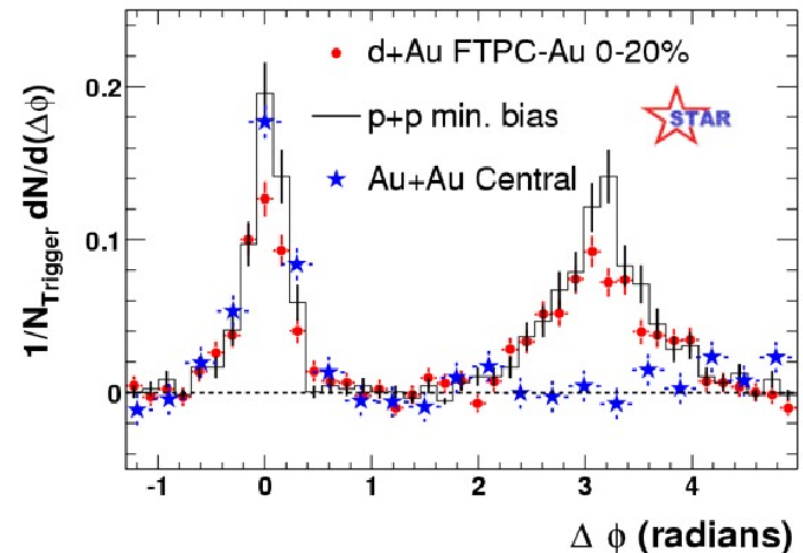
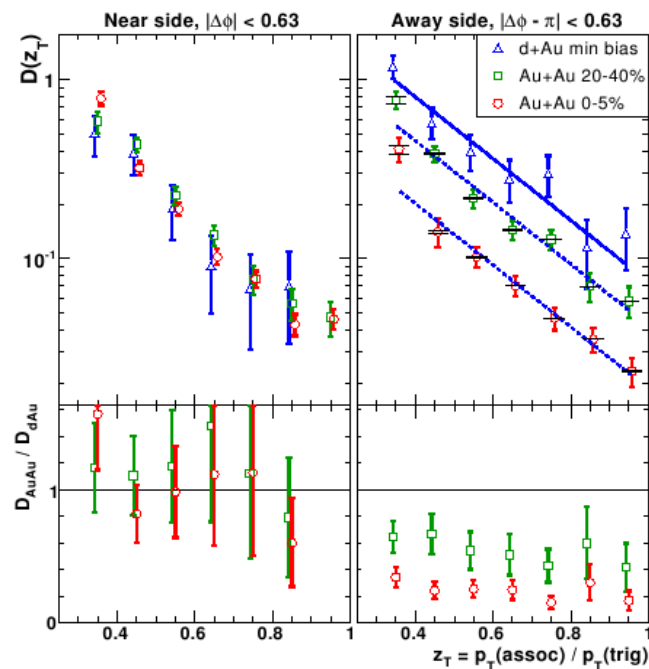
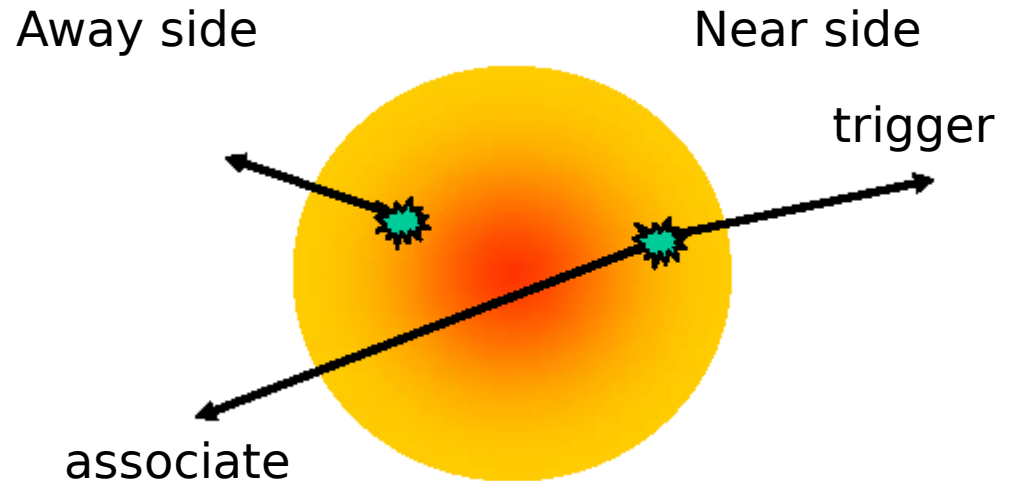
$$\rho_{WNS} = k_{WNS} \times (T_A (1 - e^{-T_B \sigma_{NN}}) + T_B (1 - e^{-T_A \sigma_{NN}}))$$

- Fragmentation: KKP



Di-hadron suppression

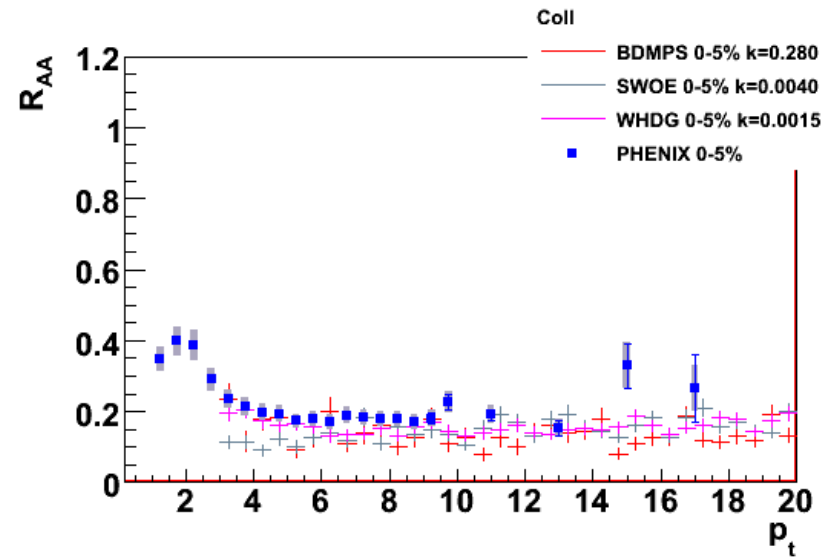
- I_{AA} : suppression of away side (associate hadrons)



R_{AA} and I_{AA}

Glauber geometry

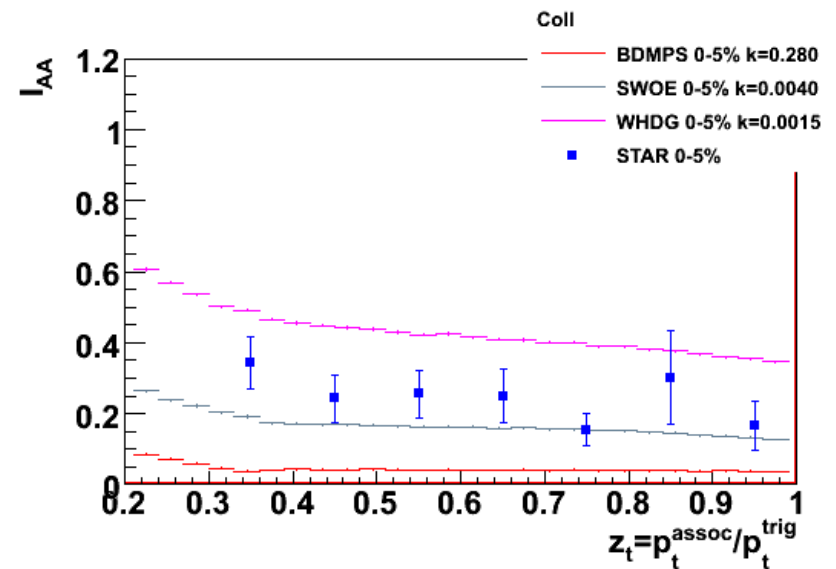
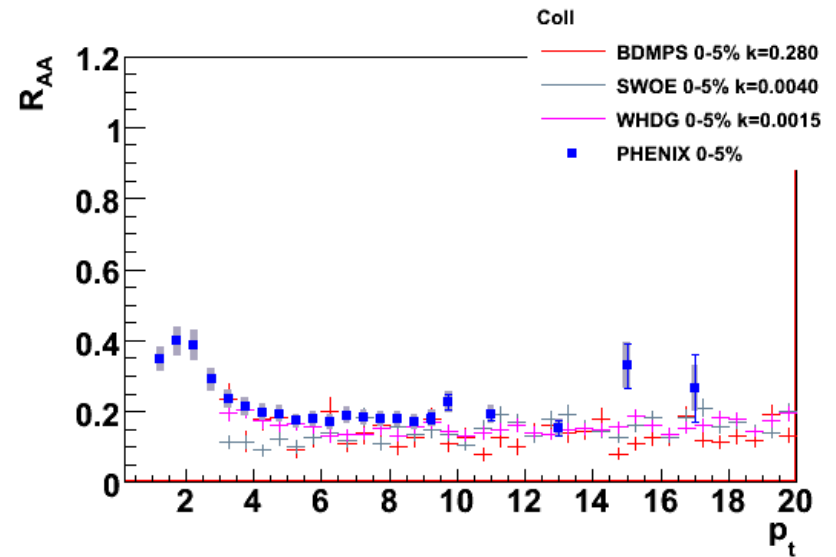
- All models can always be fitted to R_{AA} .



R_{AA} and I_{AA}

Glauber geometry

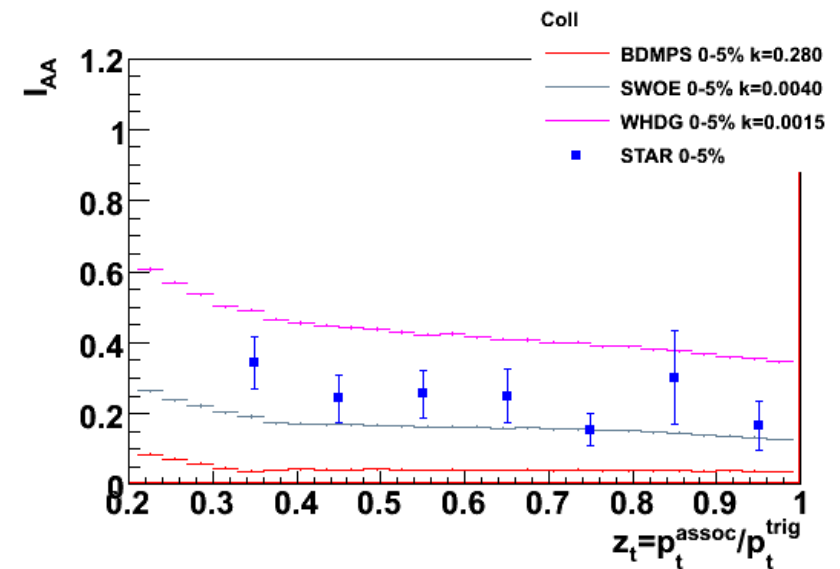
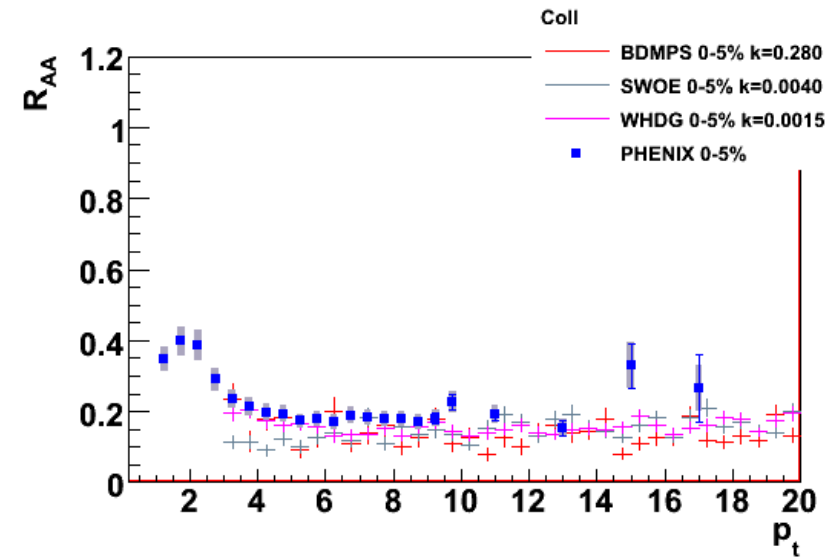
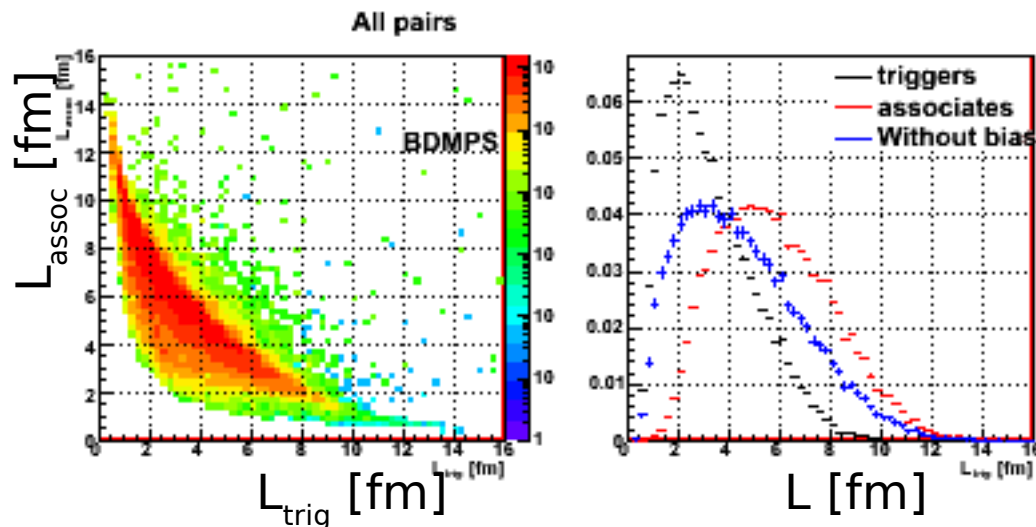
- All models can always be fitted to R_{AA} .
- Using constraint obtained from R_{AA} fit, models do not “predict” I_{AA} measurement.



R_{AA} and I_{AA}

Glauber geometry

- All models can always be fitted to R_{AA} .
- Using constraint obtained from R_{AA} fit, models do not “predict” I_{AA} measurement.

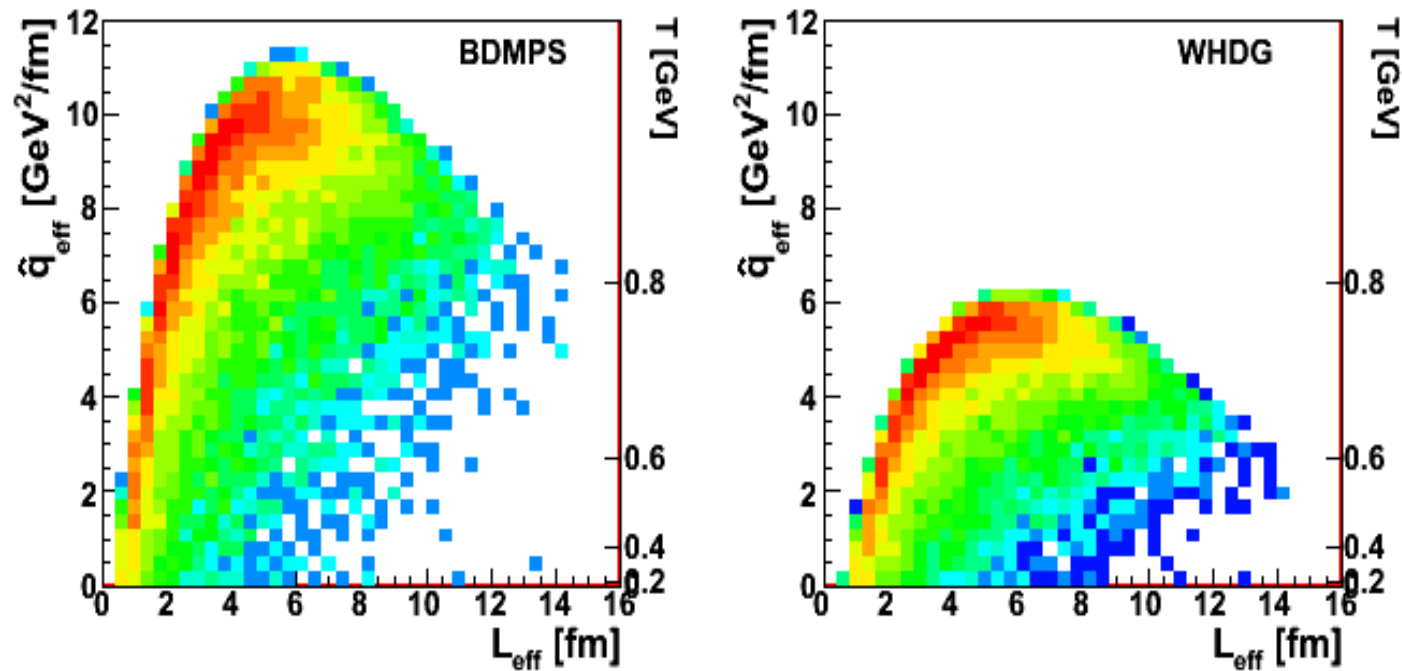


Conclusion

- All models fit RAA
- IAA can distinguish between models
- Outlook
 - Typical parton energy at RHIC: 10 GeV
 - At LHC: 100 GeV -> absorption rate lower

Backup

BDMPS vs WHDG (2)



- Scattered background: medium density for best fits collisional scaling in static medium.

Single Gluon Spectra

- **BDMPS:**

$$\omega \frac{dI}{d\omega} = \frac{\alpha_s C_R}{(2\pi)^2 \omega^2} 2\text{Re} \int_{\xi_0}^{\infty} dy_l \int_{y_l}^{\infty} d\bar{y}_l \int d\mathbf{u} \int_0^{\chi\omega} d\mathbf{k}_{\perp} e^{-i\mathbf{k}_{\perp} \cdot \mathbf{u}} e^{-\frac{1}{2} \int_{\bar{y}_l}^{\infty} d\xi n(\xi) \sigma(\mathbf{u})}$$

$$\times \frac{\partial}{\partial \mathbf{y}} \cdot \frac{\partial}{\partial \mathbf{u}} \int_{y=0}^{\mathbf{u}=\mathbf{r}(\bar{y}_l)} \mathcal{D}\mathbf{r} \exp \left[i \int_{y_l}^{\bar{y}_l} d\xi \frac{\omega}{2} \left(\dot{\mathbf{r}}^2 - \frac{n(\xi) \sigma(\mathbf{r})}{i\omega} \right) \right]$$

- **ASW-SH:**

$$\omega \frac{dI}{d\omega} = \frac{4\alpha_s C_R}{\pi} (n_0 L) \gamma \int_0^{\infty} \tilde{q} d\tilde{q} \left[\frac{\tilde{q}^2 - \sin \tilde{q}^2}{\tilde{q}^4} \right] \times \left(\frac{1}{\gamma + \tilde{q}^2} - \frac{1}{\sqrt{(\kappa^2 + \tilde{q}^2 + \gamma^2)^2 - 4\kappa^2 \tilde{q}^2}} \right)$$

- **WHDG:**

$$x \frac{dN_g}{dx} = \frac{C_R \alpha_s}{\pi} \frac{L}{\lambda} \int_0^{q_{\max}^2} \frac{2q^2 \mu^2 dq^2}{(4xE\hbar c/L)^2 + (q^2 + \beta^2)^2}$$

$$\times \int_0^{k_{\max}^2} \frac{dk^2}{k^2 + \beta^2} \frac{k^2(k^2 - q^2 + \mu^2) - \beta^2(k^2 - q^2 - \mu^2)}{((k - q)^2 + \mu^2)^{3/2} ((k + q)^2 + \mu^2)^{3/2}}$$